

Evolution of global temperature over the past two million years

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Supplementary Methods**R code for interpolation and dating uncertainty estimates for sea-surface temperature (SST) reconstructions**

As described in the Methods, this research uses a weighted average of the SST reconstruction from each time point on the 1kyr timescale (“time.new”) to interpolate each SST reconstruction (“variable.new”) to a common 1kyr timescale and to estimate dating uncertainty (“variable.new.sd”) when comparing independent records using uncertain absolute timescales (R. Samsworth was instrumental in developing this method). The following R code can be used to implement the method.

```
# Step 1: Input data
# For SST reconstruction define: 1) time ("time.old"); 2) uncertainty in time ("time.old.sd"); 3)
SST ("variable.old"); and 4) uncertainty in SST ("variable.old.sd").
# Define new timescale
time.new <- (1:2000)*1000

# Step 2: Interpolate raw SST and SST-sd estimates to the new timescale
time.old.sd.int <- spline (time.old, time.old.sd, xout = time.new)$y
variable.old.sd.int <- spline (time.old, variable.old.sd, xout = time.new)$y

# Step 3: Estimate SST at new timescale using weighted averages
variable.new <- rep(NA, length(time.new))
for (i in 1:length(time.new)) { variable.new[i] <- ksmooth (time.old, variable.old, kernel =
  "normal", bandwidth = time.old.sd.int[i], x.points = time.new[i][[2]] }

# Step 4: Estimate new variance including the variance from the dating uncertainty plus from
uncertainty in the variable
Residuals <- (variable.old %>% rep(1,length(time.new)) - rep(1,length(time.old)) %>%
  variable.new)^2
# estimating uncertainty from dating
variable.new.var.dating <- rep(NA,length(time.new))
for (j in 1:length(time.new)) {variable.new.var.dating[j] <- ksmooth (time.old,
  Residuals[,j], kernel= "normal", bandwidth= time.old.sd.int[j], x.points =
  time.new[j][[2]] }
# summing variances from both dating uncertainty and variable uncertainty
variable.new.var.total <- (variable.new.var.dating + (variable.old.sd.int)^2
  variable.new.sd <- sqrt(variable.new.var.total)
```

R code for creating global average surface temperature (GAST) reconstruction

As described in the Methods, this research estimates GAST from local SST proxy-based reconstructions, and the following R code can be used to implement the method.

```
# Step 1: Input the SST reconstructions
# Define "Temp.data" as a table of the SST estimates for each reconstruction every 1kyr using
# the method described above (2000 rows, 61 columns)
# Define "Temp.SD.data" as a table of the SST uncertainty estimate for each reconstruction
# every 1kyr using the method described above (2000 rows, 61 columns)
# Define v.latitude as the latitude for each SST reconstruction
time <- (1:2000) * 1000; tt = 2000
n.cores = 61
n.bootstrap.sim <- 2000 # number of simulations per method, resampling records and adding
# measurement noise

# Step 2: Estimate average SST values for latitudinal zones using a variety of possible spatial weighting
# schemes and combine to estimate average SST over 60°N to 60°S
# Loop over zonal methods

## Not assuming North-South Symmetry and 4 zones
# make vector of different zone definitions
latitude.zones.N.S.4 <- rbind(
  c(-30, 0, 30), #equal degrees
  c(-25.7, 0, 25.7), #equal areas
  c(-20, 0, 20),
  c(-35, 0, 35))
n.methods.sim <- dim(latitude.zones.N.S.4)[1] #simulations for each zonal boundary
# specifications
Sim.zonal.N.S.4 <- matrix (nrow = tt, ncol = n.bootstrap.sim * n.methods.sim)

#loop over lat zone definitions
for (l in 1:n.methods.sim){
  lat.zones.d <- latitude.zones.N.S.4[l,]
  lat.zones.r <- lat.zones.d * pi/180
#bootstrap for randomly selecting a record and random noise for each record ~(0,sd)
  for (i in 1:n.bootstrap.sim) {
    #creating subset
    ii <- sample (n.cores, replace = TRUE)
    Temp.ss <- Temp.data[,ii]
    Temp.SD.data.cut <- Temp.SD.data[,ii]
    v.latitude.ss <- v.latitude[ii]
    #add random noise to each core based on SD estimate per time point for each core
    Random.error <- matrix (0, nrow = tt, ncol = n.cores)
    for (j in 1:n.cores){ Random.error[,j] <- rnorm(tt, mean = 0,sd =
      Temp.SD.data.cut[,j]) }
    Temp.ss.rn <- Temp.ss[,] + Random.error

    #Calculate zonal averages with core subset and noise
```

```

dd = 1; Z1 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd])]
dd = 2; Z2 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 3; Z3 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 4; Z4 <- Temp.ss.rm[, (v.latitude.ss > lat.zones.d[dd-1])]
nn <- matrix (NA, nrow=tt, ncol=2) #add extra NA in case the set is empty,
  otherwise get errors
Temp.Z1 <- rowMeans(cbind(Z1, nn), na.rm = T)
Temp.Z2 <- rowMeans(cbind(Z2, nn), na.rm = T)
Temp.Z3 <- rowMeans(cbind(Z3, nn), na.rm = T)
Temp.Z4 <- rowMeans(cbind(Z4, nn), na.rm = T)

#Spatially-weighted average, where sum of weights is used to normalize
#Global.SST.N.S.4 record has NA for every point where at least one latitude zone
  is empty
Global.SST.N.S.4 <- (( Temp.Z1 * (sin(lat.zones.r[1]) - sin(-60 * pi/180)) +
  Temp.Z2 * (sin(lat.zones.r[2]) - sin(lat.zones.r[1]))
  + Temp.Z3 * (sin(lat.zones.r[3]) - sin(lat.zones.r[2]))
  + Temp.Z4 * (sin(60 * pi/180) - sin(lat.zones.r[3])) )
  / (2 * (sin(60 * pi/180))))
Sim.zonal.N.S.4[,i + (1-1)*n.bootstrap.sim]<- Global.SST.N.S.4
  }
}

## Not assuming North-South Symmetry and 6 zones
# make vector of different zone definitions
latitude.zones.N.S.6 <- rbind(
  c(-40, -20, 0, 20, 40), #equal degrees
  c(-35.3, -16.8, 0, 16.8, 35.3), #equal areas
  c(-30, -15, 0, 15, 30),
  c(-40, -15, 0, 15, 40),
  c(-35, -20, 0, 20, 35))
n.methods.sim <- dim(latitude.zones.N.S.6)[1] #simulations for each zonal boundary
  specifications
Sim.zonal.N.S.6 <- matrix (nrow = tt, ncol = n.bootstrap.sim * n.methods.sim)

#loop over lat zone definitions
for (l in 1:n.methods.sim){
  lat.zones.d <- latitude.zones.N.S.6[l,]
  lat.zones.r <- lat.zones.d * pi/180

#bootstrap for randomly selecting a record and random noise for each record ~ (0,sd)
  for (i in 1:n.bootstrap.sim) {
    #creating subset
    ii <- sample (n.cores, replace = TRUE)
    Temp.ss <- Temp.data[,ii]
    Temp.SD.data.cut <- Temp.SD.data[,ii]
    v.latitude.ss <- v.latitude[ii]
  }
}

```

```

#add random noise to each core based on SD estimate per time point for each core
Random.error <- matrix (0, nrow = tt, ncol = n.cores)
for (j in 1:n.cores){ Random.error[,j] <- rnorm(tt, mean = 0,sd =
  Temp.SD.data.cut[,j]) }
Temp.ss.rm <- Temp.ss[,] + Random.error

#Calculate zonal averages with core subset and noise
dd = 1; Z1 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd])]
dd = 2; Z2 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 3; Z3 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 4; Z4 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 5; Z5 <- Temp.ss.rm[, (v.latitude.ss <= lat.zones.d[dd] & v.latitude.ss >
  lat.zones.d[dd-1])]
dd = 6; Z6 <- Temp.ss.rm[, (v.latitude.ss > lat.zones.d[dd-1])]
nn <- matrix (NA, nrow=tt, ncol=2) #add extra NA in case the set is empty,
  otherwise get errors
Temp.Z1 <- rowMeans(cbind(Z1, nn), na.rm = T)
Temp.Z2 <- rowMeans(cbind(Z2, nn), na.rm = T)
Temp.Z3 <- rowMeans(cbind(Z3, nn), na.rm = T)
Temp.Z4 <- rowMeans(cbind(Z4, nn), na.rm = T)
Temp.Z5 <- rowMeans(cbind(Z5, nn), na.rm = T)
Temp.Z6 <- rowMeans(cbind(Z6, nn), na.rm = T)

#Spatially-weighted average, where sum of weights is used to normalize
#Global.SST.N.S.6 record has NA for every point where at least one latitude zone
  is empty
Global.SST.N.S.6 <- (( Temp.Z1 * (sin(lat.zones.r[1]) - sin(-60 * pi/180))
  + Temp.Z2 * (sin(lat.zones.r[2]) - sin(lat.zones.r[1]))
  + Temp.Z3 * (sin(lat.zones.r[3]) - sin(lat.zones.r[2]))
  + Temp.Z4 * (sin(lat.zones.r[4]) - sin(lat.zones.r[3]))
  + Temp.Z5 * (sin(lat.zones.r[5]) - sin(lat.zones.r[4]))
  + Temp.Z6 * (sin(60 * pi/180) - sin(lat.zones.r[5])) )
  / (2 * (sin(60 * pi/180))))
Sim.zonal.N.S.6[,i + (l-1)*n.bootstrap.sim]<- Global.SST.N.S.6
}

}

## Make the representative SST 60°N to 60°S ensemble
#first remove the ones with all the NA entries
NA.vector <- apply(Sim.zonal.N.S.4, 2, function(x) sum(is.na(x)));
Sim.zonal.N.S.4.NA1 <- Sim.zonal.N.S.4[,NA.vector != tt]
NA.vector <- apply(Sim.zonal.N.S.6, 2, function(x) sum(is.na(x)));
Sim.zonal.N.S.6.NA1 <- Sim.zonal.N.S.6[,NA.vector != tt]
ZONAL.raw <- cbind(Sim.zonal.N.S.4.NA1,Sim.zonal.N.S.6.NA1)
ZONAL.final <- ZONAL.raw[,sample(dim(ZONAL.raw)[2],2000,replace = FALSE)]

```

Step 3: Scale from latitudinal SST averages to GAST using scalars estimated from PMIP model experiments (see Methods for details), using scalars of mean 1.9 and sd 0.2 (uniform distribution is assumed)

```
n.sim <- 5000
OUTPUT.scaled <- matrix(NA, ncol = n.sim, nrow = tt)
for (j in 1:n.sim){
  zonal.scalar.value <- rnorm(1, 1.9, 0.2)
  ii <- sample(1:dim(ZONAL.final)[2], 1)
  OUTPUT.scaled[,j] <- (ZONAL.final[,ii] - mean(ZONAL.final[1:5, ii], na.rm = T)) *
  zonal.scalar.value
}
```